

geometric series	$\sum_{0 \leq k < n} x^k = \frac{1 - x^n}{1 - x}$
arithmetic series	$\sum_{0 \leq k < n} k = \frac{n(n-1)}{2} = \binom{n}{2}$
binomial coefficients	$\sum_{0 \leq k \leq n} \binom{k}{m} = \binom{n+1}{m+1}$
binomial theorem	$\sum_{0 \leq k \leq n} \binom{n}{k} x^k y^{n-k} = (x+y)^n$
harmonic numbers	$\sum_{1 \leq k \leq n} \frac{1}{k} = H_n$
sum of harmonic numbers	$\sum_{1 \leq k < n} H_k = nH_n - n$
Vandermonde convolution	$\sum_{0 \leq k \leq n} \binom{n}{k} \binom{m}{t-k} = \binom{n+m}{t}$

Table 2.2 Elementary discrete sums